

Constructive Genetic Algorithm for Machine-Part Cell Formation

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Abstract

This paper presents a new evolutionary approach to the *machine-part cell formation (MPCF) problem*, generally considered in manufacturing cell design, where a zero-one machine-part matrix must have its rows and columns moved to form machines and parts clusters. The *Constructive Genetic Algorithm (CGA)* was proposed recently to solve clustering problems, and is applied here to the *MPCF*. The *MPCF* is modeled as a bi-objective problem that guides the construction of feasible assignments of machines and parts to specify clusters, and provides evaluation of schemata and structures in a common basis. A particularly derived structure and schema representation considers *Jaccard* distances for binary strings. A variable size population is formed only by schemata, considered as building blocks for feasible solutions construction along the generations. Recombination gives population diversification, and local search mutation is applied to structures that represent feasible solutions. Experimental results are shown for instances specially generated and others taken from the literature.

Key words: genetic algorithms, manufacturing cell design, p-median problem.

1. Introduction

The international competition and its consequent needs for quick answers to the market demands have lead several companies to consider non-traditional approaches to control and design the manufacturing systems. One of these approaches is the application of the “*group technology*” [Burbidge,1969] to decompose manufacturing systems into manageable sub-systems, or groups, by aggregating similar parts into part families and machines into cells. The ideal cell is independent and completely manufactures its part family(s). Automation and control are simplified through the creation of independent cells. The production flow analysis of Burbidge [Burbidge, 1963] is one of the first and well-known methodologies associated with group technology.

There are many methods that works over a machine-part matrix with elements being zeros or ones, indicating which machines are used to produce each part. Given a matrix A (*figure 1*), where the rows corresponds to parts and columns to machines and $a_{ij} = 1$, if the part i needs the machine j to be produced. Basically, the algorithms change rows and columns positions to produce blocks of ones, forming parts families and machine cells simultaneously (*figure 2*).

Chandrasekharan and Rajagopalan [Chandrasekharan and Rajagopalan, 1989] and Venugopal and Narendran [Venugopal and Narendran, 1993] present some analysis over the zero-one matrix to extract properties and to advise for cell formation algorithms. Other algorithms following these lines can be viewed in the papers of McCormick [McCormick Jr., Schweitzer and White, 1972], King [King, 1980; King and Nakornchai, 1982] and Chu and Tsai [Chu and Tsai, 1990].

Many other techniques have been proposed in literature. Hierarchical clustering methods (Stanfel, 1985 and McAuley, 1972), non-hierarchical clustering (Chandrasekharan and Rajagopalan, 1986), graph based techniques (Rajagopalan and Batra, 1975), neural networks (Malave and Ramchandran, 1991), fuzzy logic (Xu and Wang, 1989) and *metaheuristics* like Simulated Annealing (Boctor, 1991 and Venugopal, and Narendran, 1992) and Genetic Algorithms (Joines, 1993).

Genetic Algorithms (*GAs*) are very well known, having several applications to general optimization and combinatorial optimization problems [Davis,1991; De Jong, 1975; Goldberg, 1989; Holland, 1975; Michalewicz, 1996]. A typical *GA* is based on the controlled evolution of a structured population, recombination operators and the schema formation and propagation over generations.

This paper presents an application of a *Constructive Genetic Algorithm (CGA)* to solve the *MPCF* problem. The application is made through an analogy with the *p*-median problem, since both are clustering problems. The search for *p* median vertices on a network (graph) is a classical location problem. The objective is to locate *p* facilities (medians) minimizing the sum of the distances from each demand point to its nearest facility. Very good results were obtained by Lorena and Furtado [Lorena and Furtado, 1998] using the *CGA*.

The *MPCF* is modeled as a bi-objective *p*-median problem that is used as a basis to construct feasible assignments of machines and parts to specified clusters, and considers evaluation of schemata and structures in a common basis. A particularly

derived structure and schema representation considers *Jaccard* distances for binary strings. A variable size population is formed only by schemata, considered as building blocks for feasible solutions construction along the generations. Recombination gives population diversification, and a kind of local search mutation is applied to the generated structures representing feasible solutions.

A *CGA* review is presented in section two, detailing the schemata representation, *CGA* modeling, *fg-fitness* and the evolution process, and the selection, recombination and mutation process. Section three presents computational tests considering two instances from the literature and specially generated instances, providing insights about the *CGA* performance on instances of increasing difficulty.

2. CGA review

The *CGA* is proposed to address the problem of evaluating schemata and structures in a common basis. While in the other evolutionary algorithms, the evaluation of individuals is based on a single function (the fitness function), in *CGA* this process relies on two functions, mapping the space of structures and schemata onto \mathfrak{R}_+ .

We resume the *CGA* in this section (for a complete description see the paper of Lorena and Furtado [Lorena and Furtado, 1998, http://www.lac.inpe.br/~lorena/cga/cga_clus.PDF]).

2.1 Representation

For *schema representation*, it was used a string of $n+m$ symbols, where n is the number of parts (or rows in the original matrix) and m is the number of machines (or

columns in the matrix). Each of the two portions of the schema evolves independently from each other. This application considers only one part family for each machine cell. The number k of clusters (part families or machine cells) to be formed must be defined *a priori*.

The schemata have in each position one of the following three possible symbols:

1, to indicate a median part;

0, to indicate a non-median part assigned to its nearest median; and

#, to indicate a non-median part not yet assigned to a median.

Then, both portions of the schemata (parts and machines) must have exactly k positions with the symbol 1 and the rest with 0's or #'s. A schema with no #'s is an *structure* that represents a feasible solution, where every non-median part is assigned to its nearest median, and the same for the columns.

For instance, if we need to form three manufacturing cells, a schema for a problem with 10 parts and 15 machines could be represented by

$$s_i = (0,1,\#,1,0,\#,1,0,\#,0 / 0,0,1,\#,0,1,\#,1,\#,0,0,0,\#,0).$$

Where the first 10 symbols represent parts and the last 15 symbols represent machines. Let $V_1^p(s_i) = \{2,4,7\}$ be the median part set, $V_2^p(s_i) = \{1,5,8,10\}$ the assigned non-median part set, and for machines, $V_1^m(s_i) = \{3,7,9\}$, $V_2^m(s_i) = \{1,2,6,11,12,13,15\}$.

Using the following notation: $V_1^p(s_i) = \{\mathbf{z}_1^p, \dots, \mathbf{z}_k^p\}$ and $V_1^m(s_i) = \{\mathbf{z}_1^m, \dots, \mathbf{z}_k^m\}$, the part clusters will be formed assigning elements from $V_2^p(s_i)$ to elements from $V_1^p(s_i)$ and the machine clusters assigning elements from $V_2^m(s_i)$ to elements from $V_1^m(s_i)$. The

assignment of each element from $V_2^p(s_i)$ to the nearest element from $V_1^p(s_i)$ (each element from $V_2^m(s_i)$ to the nearest from $V_1^m(s_i)$) is made based on the *Jaccard distance* among them (represented here by $\mathbf{m}_{z,q}$).

The *Jaccard* similarity coefficient for two binary strings is defined as the number of positions with value 1 in both sequences divided by number of positions with value 1 in both or one of the sequences. This coefficient is used as a "distance" measure subtracting it from one.

The part clusters $C_1^p(s_i), C_2^p(s_i), \dots, C_k^p(s_i)$ and machine clusters $C_1^m(s_i), C_2^m(s_i), \dots, C_k^m(s_i)$ are formed after the assignments.

2.2. CGA modeling

Let \mathcal{C} be the set of all structures and schemata that can be generated by the 0-1-# string representation of *section 2.1.*, and consider two functions f and g , defined as $f: \mathcal{C} \rightarrow \mathbb{R}_+$ and $g: \mathcal{C} \rightarrow \mathbb{R}_+$ such that $f(s_i) \leq g(s_i)$, for all $s_i \in \mathcal{C}$. We define the double fitness evaluation of a structure or schema s_i , due to functions f and g , as *fg-fitness*.

The *CGA* optimization problem implements the *fg-fitness* considering two objectives:

(*interval minimization*) Search for $s_i \in \mathcal{C}$ of minimal $\{g(s_i) - f(s_i)\}$,

and

(*g maximization*) Search for $s_i \in \mathcal{C}$ of maximal $g(s_i)$.

The optimization objectives of the *MPCF* problem must be reflected on the interval minimization problem. The second objective reflects the constructive phase of a *CGA*, as the schema representation drives the *fg-fitness* evaluation to increase as the number of labels # decreases and therefore structures have higher *fg-fitness* evaluation than schemata.

To attain these purposes, a problem to be solved using *CGA* is modeled as the following *Bicriterion Optimization Problems (BOP)*:

$$\begin{aligned}
 & \text{Min} \quad \{g(s_i) - f(s_i)\} \\
 & \text{Max} \quad g(s_i) \\
 & \text{subj. to} \quad g(s_i) \geq f(s_i) \\
 & \quad \quad \quad s_i \in \mathbf{C}
 \end{aligned}$$

Functions f and g must be properly identified to represent optimization objectives of the problems at issue.

2.3. The fg-fitness

In general terms, after the formation of clusters $C_1^p(s_i), C_2^p(s_i), \dots, C_k^p(s_i)$ and $C_1^m(s_i), C_2^m(s_i), \dots, C_k^m(s_i)$, the function f and the function g are computed as follows:

$$g(s_i) = \sum_{j=1}^k \sum_{q \in C_j^p(s_i)} \mathbf{m}_{z_j q} + \sum_{j=1}^k \sum_{q \in C_j^m(s_i)} \mathbf{m}_{z_j q}, \text{ and}$$

$$f(s_i) = g(s_i) - \sum_{j=1}^k \max_{q \in C_j^p(s_i)} \{m_{j,q}\} - \sum_{j=1}^k \max_{q \in C_j^m(s_i)} \{m_{j,q}\}$$

A common upper bound to f and g will be necessary at the evolution process (see 2.4.). To compute this upper bound g_{max} , in the very beginning of the process, a structure s_{random} representing a feasible solution (no #'s) is randomly generated and $g(s_{random})$ is taken as the g_{max} value.

For all computational tests, an initial population was randomly created with 20% of the rows and columns in each schema with symbols 0 and exactly k (number of part families or machine cells) with symbols 1.

2.4. The evolution process

The evolution process in *CGA* is conducted to attain the objectives (*interval minimization and g maximization*) of the *BOP*. At the beginning of the process, two *expected values* are given to these objectives, a non-negative real number $g_{max} > \text{Max}_{s_i \in X} g(s_i)$, that is an upper bound to $g(s_i)$, for each $s_i \in X$, and the interval length $d g_{max}$, obtained from g_{max} using a real number $0 < d \leq 1$.

The evolution process is then conducted considering an adaptive rejection threshold, which contemplates both objectives in *BOP*. Given a parameter $\alpha \in [0, 1]$, the expression

$$g(s_i) - f(s_i) \leq d g_{max} - \alpha \cdot d [g_{max} - g(s_k)] \quad (2.4.1)$$

presents a condition for rejection from the current population of a schema or structure s_i .

The right hand side of (2.4.1) is the threshold, composed of the expected value to the interval minimization $d g_{\max}$, and the measure $[g_{\max} - g(s_k)]$, that shows the difference of $g(s_i)$ and g_{\max} evaluations. For $\mathbf{a} = 0$, (2.4.1) is equivalent to comparing the interval length obtained by s_i and the expected length $d g_{\max}$. Schemata or structures are discarded if expression (2.4.1) is satisfied. When $\mathbf{a} > 0$, schemata have higher possibility of being discarded than structures, as structures present, in general, smaller differences $[g_{\max} - g(s_k)]$ than schemata.

Parameter \mathbf{a} is related to time in the evolution process. Considering that the good schemata need to be preserved for recombination, the *evolution parameter* \mathbf{a} starts from 0, and then increases slowly, in small time intervals, from generation to generation. The population at the evolution time \mathbf{a} , denoted by P_a , is dynamic in size according to the value of the adaptive parameter \mathbf{a} , and can be emptied during the process.

The parameter \mathbf{a} is now isolated in expression (2.4.1), thus yielding the following expression and corresponding rank to s_i :

$$\mathbf{a} \geq \frac{d g_{\max} - [g(s_i) - f(s_i)]}{d [g_{\max} - g(s_i)]} = \mathbf{d}(s_i).$$

At the time they are created, structures and/or schemata receive their corresponding rank value $d(s_i)$. The *rank* of each schema or structure is compared with the current evolution parameter a . At the moment a structure or schema is created, it is then possible to have some figure of its survivability. The higher the value of $d(s_i)$, and better is the structure or schema to the *BOP*, and they also have more surviving and recombination time.

2.5. Selection and recombination

The population is kept ordered according to "completeness" of the schema, i.e., the number of labels #s, and the schema fg-fitness. The schemata in population P_a are non-decreasing ordered using the following key

$$\Delta(s_i) = \frac{1 + d_i}{n(s_i)},$$

where $n(s_i)$ is the number of labels different from # in s_i , and $d_i = \frac{[g(\text{si}) - f(\text{si})]}{g(\text{si})}$.

The method used for selection takes the first schema from the best part of the population (*base*) and the second one from the whole population (*guide*). Before recombination, the first schema is complemented to generate a structure representing a feasible solution, i.e., all #'s are replaced by 0's. This complete structure suffers mutation and is compared to the best one found so far. Only the best one is kept along the process. The recombination merges information from both selected schemata, but preserves the number of medians in both portions (parts and machines) of the new generated schema or structure. If it is a new schema then it is inserted into the population, otherwise it suffers mutation and is compared to the best one found so far.

The recombination is best described in the following. The assignment operations must be performed in that order.

RECOMBINATION

$$\begin{aligned}
 &S_{base}(j) = \# \text{ and } S_{guide}(j) = \# \text{ then } S_{new}(j) \leftarrow \# \\
 &S_{base}(j) = 1 \text{ and } S_{guide}(j) = 1 \text{ then } S_{new}(j) \leftarrow 1 \\
 &S_{base}(j) = 0 \text{ and } S_{guide}(j) = 0 \text{ then } S_{new}(j) \leftarrow 0 \\
 &S_{base}(j) = 1 \text{ and } S_{guide}(j) = \# \text{ then } S_{new}(j) \leftarrow 1 \\
 &S_{base}(j) = 0 \text{ and } S_{guide}(j) = \# \text{ then } S_{new}(j) \leftarrow 0 \\
 &S_{base}(j) = \# \text{ and } S_{guide}(j) = 0 \text{ then } S_{new}(j) \leftarrow 0 \\
 &S_{base}(j) = \# \text{ or } 0 \text{ and } S_{guide}(j) = 1 \text{ then} \\
 &\quad S_{new}(j) \leftarrow 1 \text{ and } S_{new}(k) \leftarrow 0 \text{ for some } S_{new}(k) = 1 \\
 &S_{base}(j) = 1 \text{ and } S_{guide}(j) = 0 \text{ then} \\
 &\quad S_{new}(j) \leftarrow 0 \text{ and } S_{new}(k) \leftarrow 1 \text{ for some } S_{new}(k) = 0
 \end{aligned}$$

The mutation process used was a technique that implements successive changes in the median position inside each cluster followed by cluster reconstruction made by vertex reallocation. The following pseudo-code is more illustrative.

MUTATION

Begin:

$S' \leftarrow S;$

For each part cluster in S'

 Move the median to the cluster vertex which gives the minimum distance sum in the cluster;

For each machine cluster in S'

 Move the median to the cluster vertex which gives the minimum distance sum in the cluster;

If S is better than S'

 return $S;$

else

$S'' \leftarrow S'$ with non-median vertex reallocation;

 If S'' is better than S'

$S \leftarrow S'';$

 Goto Begin;

 else

 return $S';$

End:

At each generation, after new schemata insertion, the population is scanned to remove all schemata satisfying the condition $\mathbf{a} \geq \alpha(S_i)$. As described earlier in this paper, the evolution parameter \mathbf{a} is initially set to zero and slowly increased at each generation.

2.6. The algorithm

The Constructive Genetic Algorithm can be summed up by the pseudo-code:

CGA

Given g_{max} and d ;
 $\alpha := 0$;
 $\varepsilon := 0.05$; { time interval }
Initialize P_α ; { initial population }
Evaluate P_α ; { fg-fitness }
For all $s_i \hat{I} P_a$ compute $\mathbf{d}(s_i)$ { rank computation }
end_for
While (not stop condition) **do**
 For all $s_i \hat{I} P_a$ satisfying $\alpha < \mathbf{d}(s_i)$ **do** { evolution test }
 $\alpha := \alpha + \varepsilon$;
 Select P_α from $P_{\alpha-\varepsilon}$; { reproduction operator }
 Recombine P_α ; { recombination operators }
 Evaluate P_α ; { fg-fitness }
 end_for
 For all new $s_i \hat{I} P_a$ compute $\mathbf{d}(s_i)$ { rank computation }
 end_for
end_while

3. Experimental Results

Most of the problem instances were randomly generated for the computational tests. From the literature were taken two instances, one of them with a 20x35-part/machine matrix (Burbidge, 1969) and the other one with a 40x100 matrix (Chandrasekharan and Rajagopalan, 1989).

For *performance measure* was considered a coefficient that takes into account the number of zeros inside the clusters and the number of ones outside the clusters, respectively representing the cluster compactness and intercellular movement:

$$Coef = \frac{e - e_1}{e + e_0}$$

where: e = number of 1's in the matrix
 e_0 = number of 0's inside the clusters
 e_1 = number of 1's outside the clusters

The ideal coefficient value is 1 (no zeros inside and no ones outside the clusters), and better clustering has greater coefficient value.

To generate the instances, the number of parts, number of machines, within-cellular density (*WCD*) and inter-cellular density (*ICD*) were specified. The *WCD* is the ratio between the number of 1's inside the cluster and its size. The *ICD* is the ratio between the number of 1's outside the clusters and the number of matrix elements outside any cluster. Initially the matrix is generated with the clusters as specified, and then the matrix is perturbed randomly changing the rows and columns positions. The final form of the matrix can be used for the algorithm test.

Table 1 shows the results obtained with the instances taken from the literature, with three runs for each instance. The performance coefficient values obtained were the same best values found in the literature [Joines, 1993].

Table 2 shows the results obtained on randomly generated instances that differ from each other by the inter-cellular density. The purpose was basically verifying the algorithm sensibility under different inter-cellular densities. The performance coefficient values obtained can be compared to the values for the original cluster formation, computed previously by the instance generation program.

Table 3 shows the results obtained with randomly generated instances with different within-cellular density. Also, the purpose was verifying the algorithm sensibility.

Table 1 shows that *CGA* can obtain results as good as those listed in the literature for the two instances being considered. Results in *Table 2* were obtained with several instances of the same size, same *WCD* and increasing *ICD*. *Table 3* show results obtained with several other instances of the same size, same *ICD* and increasing *WCD*. In both cases, it seems to indicate that *ICD* and *WCD* has no effect over *CGA* performance.

All the tests were made using $\epsilon=0.01$ as the α increment, and $d = 0.1$ as the overall proportional deviation from g_{\max} .

4. Final considerations

This work describes an application of the *Constructive Genetic Algorithm* - *CGA* proposed by Lorena and Lopes [Lorena and Lopes, 1996] to the clustering formation of parts and machines in manufacturing cells. The *CGA* provides the following new features to genetic algorithms, such as the direct evaluation of schemata, population dynamic in size and formed only by schemata and the new *fg-fitness* process.

The computational results obtained were very good; presenting performance measure values as good as those listed in the literature. The algorithm seems to be unaffected by within-cellular density or inter-cellular density variation.

Acknowledgments:

The second author acknowledges Conselho Nacional de Desenvolvimento Científico e Tecnológico - CNPq (proc. 350034/91-5, 520844/96-3, 680082/95-6) and Fundação para o Amparo a Pesquisa no Estado de S. Paulo - FAPESP (proc. 95/9522-0 e 96/04585-6) for partial financial support.

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<i>Instance</i>	<i>Part/ Machine</i>	<i>Cells</i>	<i>Coef Literature</i>	<i>Coef CGA</i>
<i>Burbidge</i>	20/35	4	0.7571	0.7571
				0.7571
				0.7571
<i>Chandra</i>	40/100	10	0.8403	0.8403
				0.8403
				0.8403

Table 1: Tests using instances from the literature

<i>Instance</i>	<i>Part/ Machine</i>	<i>Cells</i>	<i>WCD</i>	<i>ICD</i>	<i>Coef Original</i>	<i>Coef CGA</i>
<i>W80i02</i>	<i>20/35</i>	<i>4</i>	<i>0.8</i>	<i>0.02</i>	<i>0.7527</i>	<i>0.7527</i>
						<i>0.7527</i>
						<i>0.7527</i>
<i>W80i03</i>	<i>20/35</i>	<i>4</i>	<i>0.8</i>	<i>0.03</i>	<i>0.7330</i>	<i>0.7330</i>
						<i>0.7330</i>
						<i>0.7330</i>
<i>W80i05</i>	<i>20/35</i>	<i>4</i>	<i>0.8</i>	<i>0.05</i>	<i>0.6931</i>	<i>0.6931</i>
						<i>0.6931</i>
						<i>0.6931</i>
<i>W80i10</i>	<i>20/35</i>	<i>4</i>	<i>0.8</i>	<i>0.10</i>	<i>0.6140</i>	<i>0.6140</i>
						<i>0.6140</i>
						<i>0.6140</i>

Table 2: Tests for ICD sensibility

<i>Instance</i>	<i>Part/ Machine</i>	<i>Cells</i>	<i>WCD</i>	<i>ICD</i>	<i>Coef Original</i>	<i>Coef CGA</i>
W70i02	20/35	4	0.7	0.02	0.6398	0.6398
						0.6398
						0.6398
W80i02	20/35	4	0.8	0.02	0.7527	0.7527
						0.7527
						0.7527
W90i02	20/35	4	0.9	0.02	0.8280	0.8280
						0.8280
						0.8280

Table 3: Tests for WCD sensibility

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	0	0	0	0	0	0	0	1	0	0	1	0	1	1	0
1	1	0	1	0	1	0	0	0	0	1	0	0	1	0	0
2	1	1	0	0	0	0	0	0	1	0	0	0	0	0	0
3	0	0	1	0	1	1	0	0	0	1	0	0	0	0	0
4	0	1	0	1	1	0	1	0	1	0	0	1	0	0	0
5	0	1	0	1	0	0	0	0	0	0	0	1	0	0	0
6	0	1	0	1	0	0	1	0	1	0	0	1	0	0	0
7	0	0	0	0	0	0	0	0	0	0	1	0	0	1	1
8	0	0	0	0	0	0	0	1	0	0	0	0	1	1	1
9	0	0	1	0	1	0	0	0	1	0	0	0	0	0	0

Figure 1: Original part-machine matrix

	1	3	6	8	11		0	2	4	5	9		7	10	12	13	14
1							1	1	1		1				1		
3								1	1	1	1						
9								1	1		1						
2	1				1		1										
4	1	1	1	1	1				1								
5	1	1			1												
6	1	1	1	1	1												
0													1	1	1	1	
7														1		1	1
8													1		1	1	1

Figure 2: Processed part-machine matrix

Captions to illustrations

Figure 1: Original part-machine matrix

Figure 2: Processed part-machine matrix