**Demad Response Model Development for Smart Households using Time of Use Tariffs and Optimal Control; The Isle of Wight Energy Autonomous Community Case Study**

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Received: date; Accepted: date; Published: date

**Abstract:** Residential variable energy price schemes can be made more effective with the use of a Demand Response (DR) strategy along with smart appliances. Using DR, the electricity bill of participating customers/households can be minimized, while pursuing other aims such as demand-shifting and maximizing consumption of locally generated renewable-electricity. In this article, a two-stage optimization method is used to implement the DR scheme. The model considers a range of novel smart devices/technologies/schemes, connected to smart-meters and a local DR-Controller. A case study with various decarbonisation scenarios were performed to analyse the effects of applying the proposed DR-scheme in households located in the west area of the Isle of Wight (Southern United Kingdom). There are approximately 15,000 households, of which 3,000 are not connected to the gas-network. Using a distribution network model along with a load flow software-tool, the secondary voltages and apparent-power through transformers at the relevant substations are computed. The results show that in summer, participating households could export 6.4MW power as a revenue, which is 10% of installed large-scale photovoltaics (PV) capacity on the island. Average CO2e reductions of 7.1ktons/annum and a reduction in combined energy/transport fuel-bills of 60%/annum could be achieved by participating households.

**Keywords:** demand response; electric vehicle; solar photovoltaics; battery; optimisation; non-linear programming; sustainability

**Nomenclature**

CO2e Carbon Dioxide Equivalent
COE Cost of Electricity
COH Cost of Heating
COV Cost of Vehicle
Introduction

To reduce the load on the grid during peak-demand periods or to maximize the use of clean energy, variable energy price schemes have been suggested [1, 2, 3]. These schemes can provide a reduced cost of electricity during off-peak consumption, or when surplus energy is being generated that would otherwise be lost [2]. Variable pricing can be more effective with the use of Demand Response (DR) strategy along with smart appliances. DR is a scheme that enables changes in the electricity usage by end-use customers in response to signals from the electricity supplier, or changes in the price of electricity over time [4]. DR enables shifts in demand patterns that can be useful for the operation of the power grid [5]. Peak demand can be reduced and shifted to off-peak periods or matched to the pattern of local generation. Using DR, the electricity bill of participating customers can be reduced and they can benefit from other incentives offered by the supplier [6]. It is clear that the home energy management sector is evolving at a fast rate, with a growing number of ‘smart’ energy devices – including for instance smart home heating controls, smart lighting and appliance controls, energy generation devices such as photovoltaics (PV) panels, and storage products – now becoming available on the market [7, 8]. DR has the potential to promote multiple benefits across all stakeholders. A reduction in energy cost to the customer could be created, with a revenue generation for prosumers. An increase in localised generation capacity to the supplier with a reduced distribution reinforcement cost to the Distribution Network Operator (DNO). Combined, energy savings can result in a reduction in greenhouse gas (GHG) emissions, essential if the UK is to meet its Paris agreement obligations and the Government’s “Net Zero” target [9]. For example, the UK government has produced a recent report which raises these points [10]. The same report indicates that there are risks as well in terms of the potential for energy rebound effects (an unintended increase in demand at certain periods), vulnerability to changes in energy pricing, and data security implications. Moreover, there may be potential barriers to the deployment of home energy controls, and new challenges for other stakeholders in the energy ecosystem, such as DNOs, energy suppliers and generators. A number of barriers to the uptake of home energy controllers, or to the realisation of their possible benefits, have been identified [10]. These barriers can be categorised as follows: (i) Technical barriers, (ii) Interoperability of equipment and standardization, (iii) Security and privacy concerns, (iv) Economic considerations, (v) Regulatory and market barriers, (vi) Consumer behaviour and awareness, and (vii) Barriers related to the smart meter rollout.

The application of DR strategies has been investigated to schedule the operation of: space heating systems [11], electric water heating systems [12], heat pumps [13], photovoltaics-battery systems [14], wind energy generation [15], solar hot water systems [16], washing machines and
dishwashers [17]. Various approaches have been used for modelling such as the Markovian model [18], game theory [19], the home energy management system (HEMS) model [20], mixed integer linear programming [21] and the ant colony optimisation algorithm [22]. At present, there are no DR models that incorporate all the commercially available DR functions, combined with the ability to differentiate property size/ use on a community-sized area.

In the current work, a DR model is described for the application of complete households incorporating key DR features, such as an electric vehicle (EV) as a potential-detachable battery bank, ability to export electricity to generate revenue and time of use tariffs in addition to rooftop PV, household battery bank, electric storage heaters, electric water heaters, smart meters and DR controller. A two-stage optimisation method is used with a gradient-based nonlinear programming algorithm, and continuing the solution with a direct search optimisation, as this can deal with situations where the underlying functions are non-differentiable, which can occur given the nature of the functions involved in the formulation of the problem.

A case study outlining the effects of applying a DR scheme in households located in the West Wight area of the Isle of Wight (IoW) are investigated with six de-carbonisation scenarios using the DR model developed and described within this article.

**Methodology**

Households are considered to adopt an appropriate subset of the following devices, technologies, or schemes (Fig. 1), so that they can participate in the DR scheme:

2.1. **Time of Use Tariff**

A Time of Use (TOU) tariff defines variable energy prices for the customer that change typically on half-hourly intervals and are updated every day. The information about tariffs is typically sent to customers via a smartphone app. TOU tariffs require a smart meter to be installed in the household, so that consumption can be metered at the required intervals. Moreover, the customer needs to opt-in for smart meter readings at the appropriate intervals. TOU can provide low prices for off peak consumption, or when cheap energy is being generated.

2.2. **Controllable Electric Storage Heaters**

A reduced price for off-peak consumption can be applied to electric storage heaters (Fig. 2). Storage heaters accumulate heat during off-peak periods and release it when required. Efficient state-of-the-art fan assisted storage heaters with low losses have been considered. The number and size of heaters depend on house type.
Figure 2. Illustration of electrical bus in the household, the different elements connected to it and the
directions of power flows. The vertical line represents a connection bus in the households, the arrows
indicate the possible direction(s) of the power flow and the switch in the electric vehicle indicates that
it can be connected or disconnected at different times of the day.

2.3. Immersion Heaters

Immersion heater with storage is an electric water heater that sits inside a hot-water cylinder. Water is heated up during off-peak periods and stored in an insulated cylinder. Heating cycles can be controlled by a DR scheme. Highly insulated cylinders with negligible losses have been considered and moreover, their size is estimated to be sufficiently large to avoid the need for ‘on-peak’ top-ups of energy.

2.4. Rooftop PV

The household solar generation, where available, is assumed to offset the additional electricity load brought about by the charging of electric vehicles and/or the installation of electric heaters. Moreover, electricity generated by PV panels can help reduce the local consumption of grid electricity, and even generate an income by exporting electricity, where a local energy market is available.

2.5. Residential Battery Storage

Residential battery storage allows the storage of energy from rooftop PV or from the grid at times when the cost of electricity is reduced. The stored energy can later be used to supply local loads. Domestic battery storage technologies adopted within this study will include an inverter as seen within the current market. This will allow the batteries to be readily integrated into the domestic system. Their charging/ discharging cycles can be controlled as part of the DR scheme.

2.6. Residential EV Charging

EV charging points with vehicle-to-grid (V2G) capability are available in some households that have adopted electric vehicles (Fig. 2). The charging/discharging of EV batteries of connected vehicles can be controlled as part of the DR scheme. When the vehicle is at home, it can be used as a temporary storage resource for the household. The stored energy in the EV battery can be used to supply local loads, and it can even be exported to the grid.

2.7. Smart Thermostats and DR controllers

The use of state-of-the-art Internet enabled automation technology, such as If-this-then-that (IFTTT), allows the control of key electric loads based on TOU price signals. Current smart thermostats, such as Tado and Nest, can be used to control storage heaters based on TOU price signals by means of IFTTT. With the use of appropriate household DR controllers (or energy management
system), smart residential batteries, EV battery charging/discharging can also be coupled to the DR scheme.

2.8. Smart Meters

A smart meter is a modern type of energy meter that can send readings to the utility company via wireless communications. This can ensure more accurate energy bills relative to conventional meters with a greater sampling frequency. Smart meters provide data on energy usage to customers to help control cost and consumption. The data that smart meters send to the utility can also be used, for example, for load factor control, to analyse peak-load requirements, and for the development of pricing strategies based on consumption information dependent on the frequency and timeliness of reporting.

Currently, there are two types of smart meter in the UK: first and second-generation, which are also referred to as SMETS1 and SMETS2 (Smart Metering Equipment Technical Specification), respectively. The new generation addresses several issues associated with the first generation of smart meters and provides a range of new functionality. At present only the SMETS2 smart meter can be used in conjunction with a Time of Use tariff.

2.9. Export of Energy to Grid

The study considers that the households participate in local energy market with a scheme to enable customers to sell excess electricity by exporting it to the grid, the operations of which are beyond the scope of this study.

Demand Response Modelling

The following sub-sections describe the modelling methodology development for the above-mentioned DR technologies and methods, and the two stage optimisation algorithms:

3.1. Residential Battery

The rate of change of energy stored in battery bank is given by

\[
\frac{dE_B(t)}{dt} = \begin{cases} 
\eta_{B,C} P_B(t) & \text{if } P_B(t) \geq 0 \\
\frac{P_B(t)}{\eta_{B,D}} & \text{if } P_B(t) < 0 
\end{cases}
\]  

(1)

where \(E_B(t)\) is the energy stored in battery at any instant \(t\), \(P_B\) is the power consumed (the case when \(P_B\) is positive) or released (the case when \(P_B\) is negative) by battery, \(\eta_{B,C}\) is the battery’s charging efficiency and \(\eta_{B,D}\) is the discharging efficiency. The energy stored in battery at any instant can be calculated by

\[
E_B(t) = E_B(0) + \int_0^t \eta_B P_B(\tau) d\tau
\]  

(2)

with the following initial conditions and constraints:

\[
E_B(0th \ hour) = E_B(24th \ hour)
\]  

(3)

\[-P_{B,O} \leq P_B(t) \leq P_{B,I} \quad \forall \ t\]

(4)

\[0 \leq E_B(t) \leq E_{BC} \quad \forall \ t\]

(5)

\(\eta_B\) becomes \(\eta_{B,C}\) when \(P_B(\tau)\) is positive and it becomes \(1/\eta_{B,D}\) when \(P_B(\tau)\) is negative. \(P_{B,O}\) and \(P_{B,I}\) are the output and input power ratings of battery. \(E_{BC}\) is the storage capacity of battery. The battery can consume power from the bus and give power to the bus. Thus, \(P_B\) can be negative or positive and the bounds on the power release and consumption are conveyed by Eq. (4). Note that Eq. (3) is imposed to ensure that model solution is periodic, with a period of 24 hours, thereby reducing the window of time over which simulations must be carried out to a single day.
3.2. Rooftop PV Electricity Generation

PV electricity generation ($P_{PV}$) is defined as the electricity generated by the solar photovoltaic modules mounted at the roof of the household. The amount of power generated depends on the solar irradiance ($I$), reference temperature ($T_{ref}=25^\circ C$), reference irradiance ($I_{ref}=1000\ W/m^2$), area of solar cells (A), operating temperature of PV ($T_{PV}$), PV efficiency at reference point ($\eta_{ref}=0.1537$), temperature coefficient for PV efficiency ($\beta=-0.005K^{-1}$), irradiance coefficient for PV efficiency ($\gamma=0.085$) and other losses including inverter efficiency and cable/wiring losses ($\eta_{loss}=0.15$) [23]. Thus, the power generated by rooftop PV is estimated as follows:

$$P_{PV} = (1 - \eta_{loss})\eta_{ref}(1 + \beta(T_{PV} - T_{ref}) + \gamma \ln(1/I_{ref}))$$

(6)

3.3. Electric Storage Heater

The energy stored in the electric storage heater ($E_{SH}$) at any instant can be given by

$$E_{SH}(t) = E_{SH}(0) + \int_0^t [P_{SH}(\tau) - D_{SH}(\tau)] d\tau$$

(7)

with the following initial conditions and constraints:

$$E_{SH}(0th\ hour) = E_{SH}(24th\ hour)$$

(8)

$$0 \leq P_{SH}(t) \leq P_{SH,I} \forall t$$

(9)

$$0 \leq E_{SH}(t) \leq E_{SH,C} \forall t$$

(10)

where $P_{SH}$ is the power consumed by storage heater, $D_{SH}$ is the space heating demand, $P_{SH,I}$ is the input power rating of storage heater and $E_{SH,C}$ is the storage capacity of storage heater. The storage heater can consume power from the bus but cannot give power to the bus. Thus, $P_{SH}$ cannot be negative which is conveyed by Eq. (9).

3.4. Immersion Heater

The energy stored in immersion heater ($E_{IH}$) at any instant can be calculated by

$$E_{IH}(t) = E_{IH}(0) + \int_0^t [P_{IH}(\tau) - D_{HW}(\tau)] d\tau$$

(11)

with the following initial conditions and constraints:

$$E_{IH}(0th\ hour) = E_{IH}(24th\ hour)$$

(12)

$$0 \leq P_{IH}(t) \leq P_{IH,I} \forall t$$

(13)

$$0 \leq E_{IH}(t) \leq E_{IH,C} \forall t$$

(14)

where $P_{IH}$ is the power consumed by immersion heater, $D_{HW}$ is the hot water demand, $P_{IH,I}$ is the input power rating of immersion heater and $E_{IH,C}$ is the storage capacity of immersion heater. The immersion heater can consume power from the bus but cannot give power to the bus. Thus, $P_{IH}$ cannot be negative which is conveyed by Eq. (13).

3.5. Battery of Electric Vehicle

The energy stored in EV battery ($E_{EV}$) at any instant can be calculated by

$$E_{EV}(t) = E_{EV}(0) + \int_0^t \eta_{EV}(P_{EV}(\tau) - D_{EV}(\tau)) d\tau$$

(15)

with the following initial conditions and constraints:

$$-P_{EV,0} \leq P_{EV}(t) \leq P_{EV,I} \text{ if } t_{arr} < t < t_{dep}$$

(16)

$$P_{EV}(t) = 0 \text{ if } t_{dep} \leq t \leq t_{arr}$$

(17)
where $P_{EV}$ is the power consumed or released by battery of EV. When $P_{EV}$ is positive, EV battery consumes power and when $P_{EV}$ is negative, EV battery releases power. $\eta_{EV}$ becomes $\eta_{EV,C}$ when $P_{EV}(t)$ is positive and it becomes $1/\eta_{EV,D}$ when $P_{EV}(t)$ is negative. $\eta_{EV,C}$ is the battery’s charging efficiency and $\eta_{EV,D}$ is the discharging efficiency. $D_{EV}$ is the power demand for EV when EV is away from home. $t_{arr}$ and $t_{dep}$ are the arrival and departure timings of the EV to/from home respectively. $P_{EV,0}$ and $P_{EV,1}$ are the output and input power ratings of EV battery. $E_{EV,C}$ is the storage capacity of EV battery. The EV battery can consume power from the bus and give power to the bus when it is connected to the EV charger. Thus, $P_{EV}$ can be negative or positive and the bounds on the power release and consumption are conveyed by Eq. (16). The EV battery does not consume power from the bus nor does it give power to the bus when it is disconnected from the EV charger. Thus, the $P_{EV}$ is 0 for this time interval which is conveyed by Eq. (17). It is assumed that EVs will follow a similar use pattern as conventional fossil fuel vehicles, with an average daily mileage of 18.0 miles (29km) as reported by the UK Governments Department for Transport [24]. This is approximately 5.1kWh of the battery usage per day.

3.6. Power Consumption from the Grid and Export to the Grid

The household is able to both consume power from the grid and export power to the grid. Household power consumption/export is denoted by $P_c$. We use a sign convention so that when $P_c$ is positive, the household consumes power from grid and when $P_c$ is negative, the household exports power to grid. Household power consumption/export can be calculated by the following power balance

$$P_c(t) + P_{EV}(t) = P_b(t) + P_{SH}(t) + P_{IH}(t) + P_{EV}(t) - D_{org}(t)$$

with the following constraint:

$$-P_{G,0} \leq P_c(t) \leq P_{G,1}$$

where $D_{org}$ is the original electricity demand of the household before including the smart appliances. $P_{G,0}$ and $P_{G,1}$ are the bounds for the $P_c$. The power consumption from the grid ($P_c$) and the power export to the grid ($P_e$) can be computed as follows

$$P_c(t) = \begin{cases} P_c(t) \text{ if } P_c(t) \geq 0 \\ 0 \text{ if } P_c(t) < 0 \end{cases}$$

$$P_e(t) = \begin{cases} P_e(t) \text{ if } P_e(t) < 0 \\ 0 \text{ if } P_e(t) \geq 0 \end{cases}$$

3.7. Net Cost of Electricity

The net cost of electricity per day (COE) can be computed by subtracting the earnings due to export from the cost of consumed electricity, as follows

$$COE = \int_{0^{th\ hour}}^{24^{th\ hour}} [P_c(t) Pr_{TOU}(t) - P_e(t) Pr_{E}(t)] dt$$

where $Pr_{TOU}(t)$ is the TOU price signal value at time $t$ and $Pr_E(t)$ is the export price of electricity at time $t$.

3.8. Objective Function

This DR approach is based on the solution of an optimisation problem for each household. The optimisation problem involves the minimisation of an objective function, which is defined as the net COE per day for each household adopting the DR scheme. This minimisation is achieved by adjusting
the following decision variables: \( P_n(t) \), \( P_{so}(t) \), \( P_{ov}(t) \), \( E_n(0) \), \( E_{so}(0) \), \( E_{ov}(0) \) and \( E_{ev}(0) \) during the 24 hour period.

### 3.9. Optimisation Approach

A key underlying assumption of this study is that the DR controller receives from the energy supplier the price information in advance every day for the next 24 hour period, and then it performs an optimisation that determines the optimal values of all the decision variables over the next 24 hour period. This optimisation is performed with consideration of the objective function and decision variables defined in section 3.8, along with all required constraints that are described in sections 3.1 to 3.7. For each household, the optimisation is performed in two stages, starting with a gradient-based nonlinear programming algorithm, and continuing the solution with a direct search optimisation approach. The first method allows it to find a good solution that satisfies all constraints relatively quickly, while the second method is able to improve the first stage solution, as it can deal with situations where the underlying functions are non-differentiable, which can occur given the nature of the functions involved in the formulation of the problem.

### 3.10. Aggregation

The method to aggregate power consumption of all households in the study region is described in this sub-section. The power consumption of the households that take part in DR scheme can be calculated using Eq. (22). The power consumption of the households that do not take part in DR scheme is the same as the original electricity demand \( (D_{org}) \). The total aggregated original power consumption of the study region \( (P_{C,org,a}) \) and the one after the introduction of the DR scheme \( (P_{C,DR,a}) \) can be estimated as follows:

\[
P_{C,org,a}(t) = \sum_{i=1}^{N} D_{org}(i, t) \tag{25}
\]

\[
P_{C,DR,a}(t) = \sum_{i=1}^{N} P_{C}(i, t) \tag{26}
\]

where \( N \) is the number of households in the study region.

### 3.11. Calculation of Load Power Increments

The increment in the total power consumption \( (\Delta P) \) by all the households of the study region due to the adoption of new devices, technologies and DR scheme can be estimated as follows:

\[
\Delta P(t) = P_{C,DR,a}(t) - P_{C,org,a}(t) \tag{27}
\]

### 3.12. Reduction in Energy/Fuel Bills

The reduction in daily energy/fuel bills of the participating households can be calculated by subtracting the daily bills after DR from the original daily bills before DR. The original aggregated daily bills of the participating households before DR include the original aggregated COE per day \( (COE_{org,a}) \), aggregated cost of heating per day by gas for on-gas households \( (COH_{org,gas,a}) \), aggregated cost of heating per day by fuel for off-gas households \( (COH_{offgas,org,a}) \) and aggregated cost of fuel per day for vehicles \( (COV_{org,a}) \). The aggregated daily bills after DR include the aggregated COE per day after DR \( (COE_{DR,a}) \) and aggregated cost of heating per day by gas for on-gas households \( (COH_{org,gas,a}) \). It must be noted that the cost of heating after DR for off-gas households and the cost of fuel for vehicles after DR are already included in the COE \( (COE_{DR,a}) \) as electric heaters and electric vehicles are used after DR. Thus, the average reduction in the energy/fuel bills per day per household \( (R) \) of the participating households can be written as follows:

\[
R = (COE_{org,a} + COH_{org,gas,a} + COH_{offgas,org,a} + COV_{org,a} - COE_{DR,a} - COH_{org,gas,a}) / n \tag{28}
\]
where \( n \) is the number of households participating in the DR scheme. Before DR, the electricity tariff of £0.14 per kWh is considered and the cost of fuel used for heating in off-gas households is considered to be £0.06 per kWh of heat delivered. For fossil fuel based vehicles, mileage of 10 miles per litre is considered with fuel cost of £1.30 per litre.

### 3.13. CO\(_2\) Emissions Reduction

The reduction in the CO\(_2\) emissions achieved by participating households after DR can be calculated by the addition of CO\(_2\) emissions reductions achieved by rooftop solar electricity generation, usage of electricity instead of oil for space heating in off-gas households and usage of electric vehicles instead of petrol/diesel based vehicles.

Using the 2019 UK Government GHG conversion factors [25], the following constants for CO\(_2\)e were assumed. An average UK figure of 254 gCO\(_2\) emissions per kWh of grid electricity is considered. Thus, rooftop solar PV can provide 254 gCO\(_2\) emissions reduction per kWh of solar electricity generation. A figure of 270 gCO\(_2\) emissions per kWh of heat delivered by burning oil is considered, resulting in a CO\(_2\)e reduction of 16 gCO\(_2\)e per kWh of space heating by usage of grid electricity instead of oil. The figure will be 270 gCO\(_2\) emissions reductions per kWh of space heating if solar electricity will be used instead of oil. An average figure of 1.46 tons of CO\(_2\)e emissions reductions using EV per 10,000 miles is considered.

#### Case Study: Isle of Wight Energy Autonomous Community

In this case study, the effects of applying a DR scheme in households located in the West Wight area of the IoW are investigated as part of the IoW Energy Autonomous Community (EAC). The island is located on the south coast of England, between 3 and 8km from the mainland. The study area on the island has been selected to represent around 50,000 inhabitants, which amounts to approximately 15,000 households in the study area. Of, which 3,000 are not connected to the gas network. This DR study considers both on-gas and off-gas households. Currently all off-gas households are assumed within this study to be heated using higher cost (comparatively to on-gas properties), carbon-intensive fuels, such as on-peak electricity, oil and LPG. Households are assumed to adopt an appropriate subset of the aforementioned devices, technologies, or schemes (Fig. 1), so that they can participate in the DR scheme. For an average household, the estimated original electricity demand before including the proposed smart appliances [26], space heating demand [27], hot water demand and power generated by 3kWp PV at the study region [28] are shown in Fig. 3, for the case of summer and winter.

![Original Electricity Demand](image)

![Electricity Demand for Space Heating](image)
Due to variability in the sizes of households, their electricity consumptions differ. Moreover, the power ratings, sizes and number of storage heaters/ immersion heaters/ battery banks / PV/ EV also differ for different types of households. In this study, the variability in the household size is modelled by making use of council tax bands. Our reasoning to consider council tax bands as a proxy for energy consumption is that council tax bands correlate well with the size of the property, given this tax was established on the basis of house price at a particular year in the past, and for a given region, house prices are correlated to size. Moreover, size correlates to energy consumption since a greater household volume requires a greater amount of energy for heating during winter months. There is also increased electricity consumption due to lighting and the higher capacity for occupants in a bigger household. A greater number of occupants means a greater hot water and electricity consumption. The percentage of households in the IoW that belongs to Council Tax Band A is 14.42%. The respective values for Band B, C, D, E, F, G and H are 25.57%, 24.21%, 19.00%, 10.06%, 4.48%, 2.06% and 0.2%. Based on the given distribution of households in the council tax bands, the household of Band C represents the average household. The original electricity demand, space heating demand and water heating demands per household for Band A, B, D, E, F, G and H are 0.667, 0.833, 1.167, 1.333, 1.667, 2 and 2.333 times than that of Band C.

The increments in the total power consumption by all the households of the study region due to the adoption of new devices, technologies and DR scheme are computed within the model described above. The corresponding CO₂ emissions reduction due to the decarbonisation and reduction in bills for the participating households are also computed. The resulting load power increments are divided in equal parts into the two substations (Substations A and B) that serve the region of study (Fig. 4). Each substation has two power transformers whose secondary is a common bus which represents the connection point to the distribution feeders that supply the region of study. Subsequently, the power increments for each substation are added to the known demand profiles for the corresponding secondary buses. Using a distribution network model for the IoW, along with a load flow software tool developed by the University of Newcastle based on MATPOWER (exogenous to the model described within this paper ([32])), secondary voltages and apparent power through transformers of substations after the introduction of DR scheme are computed and compared against the original values¹ before the adoption of DR scheme. Moreover, the apparent power flows through the undersea cable interconnectors with the mainland before and after the implementation of DR are analysed, and the increments in the apparent power through the interconnectors are reported. The results are computed and analysed for six decarbonisation scenarios based on the season, and different adoption levels of DR scheme and electric vehicles.

¹ At present, it is not possible to display the original values before the adoption of DR scheme due to an embargo on the original base data.
**Figure 4.** Isle of Wight (IoW) electrical distribution system-Network Map. The IoW study area is highlighted in green. Locations of assets and routes of overhead lines, underground cables and submarine cables are approximate indications for information only. PV - Photovoltaic, MW – Megawatt, kV – Kilovolt. Image produced using data from Grontmij (2010) [29].

The study is based on the following assumptions:

1. Table 1 shows the specifications assumed in this study for the rooftop PV installation, storage heaters, immersion heaters, battery banks, and electric vehicles for all the household types.
2. The devices currently available in the market have been considered, and have sized them appropriately for the corresponding household type.
3. With regard to the specifications of the electric vehicle battery capacity, we assumed that smaller properties that have an electric vehicle will have a Nissan Leaf (or similar) with a battery capacity of 30 kWh, while larger households that have an electric vehicle will have a Tesla Model S (or similar) with a battery capacity of 70 kWh.
4. In all cases, we assumed an EV charger with a power rating of 10 kW. The larger power rating for the EV charger (compared to the entry level of 3 kW) allows greater flexibility for vehicle-to-grid (V2G) applications.
5. The specification of the rooftop PV installation is determined on the basis of household size, considering typical installations in the UK. It is assumed that only the properties participating in the DR scheme have a PV installation.
6. Each household size (as represented by the council tax band) is assumed to have devices with different ratings.
7. Time of Use Tariffs and Export Tariffs employed are shown in Table 2, and remain fixed within their time ranges as discussed within private communication with Lumeanza Gmbh [30].

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2 Lumenaza Gmbh is an SME that specialises in developing specialist algorithms and software for the sale and supply of locally produced renewable energy.
8. In the scenarios described within section 5, the central figure of 10% EV adoption assumes projected EV passenger vehicle penetration level in the UK for 2025 [31]. It is assumed in the scenarios that all houses that have an EV are participating in the DR scheme, and that there is only one EV in each of those households. Note that not all households that are part of the DR scheme are assumed to have an EV.

9. The demand data and network topology used in load flow studies correspond to the year 2017.

### Table 1. Devices specifications

<table>
<thead>
<tr>
<th>Gas connection type</th>
<th>Council tax band</th>
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<th>SH total input power rating (kW)</th>
<th>SH total output power rating (kW)</th>
<th>IH Power rating (kW)</th>
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</table>

### Table 2. Time of Use and Export Tariffs [30] (wholesale price, WHP, for electricity is 6.1 p/kWh)

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<th>Time</th>
<th>TOU Tariff Summer (p/kWh)</th>
<th>TOU Tariff Winter (p/kWh)</th>
<th>Export Tariff Summer (p/kWh)</th>
<th>Export Tariff Winter (p/kWh)</th>
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<td>WHP + 0.6 p</td>
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<tr>
<td>6 AM - 10 AM</td>
<td>16.27</td>
<td>17.5</td>
<td>WHP + 0.1 p</td>
<td>WHP + 0.6 p</td>
</tr>
<tr>
<td>10 AM - 4 PM</td>
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<td>WHP - 0.5 p</td>
<td>WHP + 0.4 p</td>
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<tr>
<td>4 PM – 11 PM</td>
<td>32.55</td>
<td>35</td>
<td>WHP - 0.2 p</td>
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### Results and Discussion

The following six decarbonisation scenarios have been considered to estimate the total power consumption by 15,000 households in the study region, apparent power flows through transformers, voltages at transformers, apparent power flows through interconnectors, CO2 emissions reduction and reduction in bills under different scenarios based on the season, percentage of the households adopting DR scheme and percentage of households having electric vehicles. With regard to the level of adoption of the DR scheme, we consider a base scenario of 40% adoption in the study region, and evaluate sensitivity by considering a higher (60%) level of adoption, and a lower (20%) level of adoption. In relation to the level of adoption of electric vehicles, we consider a central case of 10%
adoption in the study region and evaluate sensitivity by considering lower EV adoption (5%), and higher EV adoption (15%). Producing the following scenarios in Table 3:

Table 3. Description of the adoption levels of DR technologies and EV ownership within each scenario.

<table>
<thead>
<tr>
<th>Scenario number</th>
<th>Adoption level of DR scheme (%)</th>
<th>Adoption level of EV (%)</th>
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</tr>
<tr>
<td>6</td>
<td>40</td>
<td>15</td>
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5.1. Scenario 1: Winter, DR 40%, EV 10%

The increments in the total power demand by 15,000 households over a 24 hour period due to the adoption of DR and new devices are computed for winter month when 40% of the households of the study region adopt DR and 10% adopt an EV. It is found that there is an increment of 44 MWh/day. However, due to the decarbonisation, CO₂ emissions reduction of 16 tons/day and average reduction in bills of 28% are achieved by the participating households for this scenario.

The apparent power flows through transformers after implementing DR are plotted in Fig. 5 for both substations. The results show that the DR optimization has shifted the electricity demand towards late night when electricity is cheaper. The minimum apparent power flows after DR are decreased to 2.1 and 1.3 MVA for substations A and B respectively. The maximum apparent power flows after DR are increased to 15.4 and 14.2 MVA for substations A and B respectively. It is seen that even after adopting the DR and new devices, the maximum apparent power flows are 51% and 47% of the combined transformer power rating of substations A and B respectively.

![Figure 5](image_url)

Figure 5. Apparent power flows through transformers after the introduction of DR scheme for scenario 1.

Secondary voltages at transformers of both substations after the introduction of DR scheme are presented in Fig. 6a. It can be seen that the minimum and maximum voltages after DR at transformers in substation A are 0.872 p.u. and 0.965 p.u., respectively. For transformers at substation B, these values are 0.859 p.u. and 0.968 p.u., respectively. It can be seen that there are instances when the voltages are 12.8% and 14.1% below the nominal voltages for transformers at substations A and B respectively. These voltages are clearly not acceptable from an operational perspective, but there are relatively easy ways of bringing those voltages to the allowed range of +/- 6% of the nominal voltage, including the adjustment of transformer taps and reactive compensation.
The apparent power flows through the interconnectors after the implementation of DR are analysed. It is found that the maximum apparent power flow at the interconnectors after DR is decreased by 2.9%. The increments in the apparent power flow through the interconnectors after the implementation of DR are also plotted in Fig. 6b. Note that the apparent power flows through the interconnectors tend to increase between 0:00 and 7:00 (hence the positive increments) because of increased consumption in the study region driven by low electricity prices, while they decrease (negative increments) during the rest of the day partly as a result of PV generation in participating households, export of electricity from the households to the grid, the use of energy storage, and higher electricity prices.

5.2. Scenario 2: Summer, DR 40%, EV 10%

The increments in the total power demand by 15,000 households over a 24 hour period due to adoption of DR and new devices are computed for summer month when 40% of the households of the study region adopt DR and 10% adopt an EV. It is found that there is a decrement of 19 MWh/day due to excess solar electricity generation. Due to the decarbonisation, CO₂ emissions reduction of 23 tons/day and average reduction in bills of 93% are achieved by the participating households for this scenario.

The apparent power flows through transformers after implementing DR are plotted in Fig. 7 for both substations. The results show that the minimum apparent power flows after DR are decreased to 0.9 and 1.1 MVA for substations A and B respectively. The maximum apparent power flow after DR is increased to 7.0 MVA for substations A and B respectively. It is seen that even after adopting the DR and new devices, the maximum apparent power flow is 23% of the combined transformer power rating of substations A and B.

Secondary voltages at transformers of both substations after the introduction of the DR scheme are presented in Fig. 8a. It can be seen that the minimum and maximum voltages after DR at transformers in substation A are 0.934 p.u. and 0.976 p.u., respectively. For transformers at substation B, these values are 0.926 p.u. and 0.974 p.u. respectively. It can be seen that there are instances when the voltages are 6.6% and 7.4% below the nominal voltages for transformers at substations A and B respectively.

The apparent power flows through the interconnectors after the implementation of DR are analysed. It is found that the maximum apparent power flow at the interconnectors after DR is decreased by 0.9%. The increment in the apparent power flow through the interconnectors after the implementation of DR is also plotted in Fig. 8b.
Figure 7. Apparent power flows through transformers after the introduction of DR scheme for scenario 2

Figure 8. (a) Secondary voltage at transformers of both substations and (b) increment in apparent power flow through inter-connectors after the implementation of DR for scenario 2

Aggregated power export from the participating households after the implementation of DR for scenario 2 is plotted in Fig. 9. Note that the peak value of 6.4MW is about 10% of the installed large-scale solar PV generation capacity on the island.

Figure 9. Aggregated power export from the participating households after the implementation of DR for scenario 2 (summer, DR adoption level of 40%, EV adoption level of 10%)

5.3. Scenario 3: Winter, DR 60%, EV 10%

The increments in the total power demand by 15,000 households over a 24 hour period due to the adoption of DR and new devices are computed for winter month when 60% of the households of
the study region adopt DR and 10% adopt an EV. It is found that there is an increment of 59 MWh/day. However, due to the decarbonisation, CO₂ emissions reduction of 22 tons/day and average reduction in bills of 27% are achieved by the participating households for this scenario.

The apparent power flows through transformers after implementing DR are plotted in Fig. 10 for both substations. The results show that the minimum apparent power flows after DR are decreased to 1.2 and 0.4 MVA for substations A and B respectively. The maximum apparent power flows after DR are increased to 20.8 and 19.6 MVA for substations A and B respectively. It can be seen that even after adopting the DR and new devices, the maximum apparent power flows are 69% and 65% of the combined transformer power rating of substations A and B respectively.

![Figure 10](image-url)

**Figure 10.** Apparent power flows through transformers after the introduction of DR scheme for scenario 3

Secondary voltages at transformers of both substations after the introduction of DR scheme are presented in Fig. 11a. It can be seen that the minimum and maximum voltages after DR at transformers in substation A are 0.820 p.u. and 0.971 p.u., respectively. For transformers at substation B, these values are 0.798 p.u. and 0.974 p.u., respectively. It can be seen that there are instances when the voltages are 18.0% and 20.2% below the nominal voltages for transformers at substations A and B, respectively.

![Figure 11](image-url)

(a) Secondary voltage at transformers of both substations and (b) increment in apparent power flow through inter-connectors after the implementation of DR for scenario 3

The apparent power flows through the interconnectors after the implementation of DR are analysed. It is found that the maximum apparent power flow at the interconnectors after DR is decreased by 4.3%. The increment in the apparent power flow through the inter-connectors after the implementation of DR is also plotted in Fig. 11b.
5.4. Scenario 4: Winter, DR 20%, EV 10%

The increments in the total power demand by 15,000 households over a 24 hour period due to the adoption of DR and new devices are computed for winter month when 20% of the households of the study region adopt DR and 10% adopt an EV. It is found that there is an increment of 28 MWh/day. However, due to the decarbonisation, CO₂ emissions reduction of 10 tons/day and average reduction in bills of 37% are achieved by the participating households for this scenario.

The apparent power flows through transformers after implementing DR are plotted in Fig. 12 for both substations. The results show that the minimum apparent power flows after DR are decreased to 3.1 and 2.2 MVA for substations A and B respectively. The maximum apparent power flow after DR are increased to 10.7 and 9.5 MVA for substations A and B respectively. It can be seen that even after adopting the DR and new devices, the maximum apparent power flows are 35% and 32% of the combined transformer power ratings of substation A and B respectively.

![Figure 12. Apparent power flows through transformers after the introduction of DR scheme for scenario 4](image_url)

Secondary voltages at transformers of both substations after the introduction of DR scheme are presented in Fig. 13a. It can be seen that the minimum and maximum voltages after DR at transformers in substation A are 0.913 p.u. and 0.960 p.u., respectively. For transformers at substation B, these values are 0.906 p.u. and 0.961 p.u., respectively. It can be seen that there are instances when the voltages are 8.7% and 9.4% below the nominal voltages for transformers at substations A and B, respectively.

![Figure 13. (a) Secondary voltage at transformers of both substations, and (b) increment in apparent power flow through inter-connectors after the implementation of DR for scenario 4](image_url)
The apparent power flows through the interconnectors after the implementation of DR are analysed. It is found that the maximum apparent power flow at the interconnectors after DR is decreased by 1.5%. The increment in the apparent power flow through the interconnectors after the implementation of DR is also plotted in Fig. 13b.

5.5. Scenario 5: Winter, DR 40%, EV 5%

The increments in the total power demand by 15,000 households over a 24 hour period due to the adoption of DR and new devices are computed for winter month when 40% of the households of the study region adopt DR and 5% adopt an EV. It is found that there is an increment of 37 MWh/day. However, due to the decarbonisation, CO$_2$ emissions reduction of 14 tons/day and average reduction in bills of 23% are achieved by the participating households for this scenario.

The apparent power flows through transformers after implementing DR are plotted in Fig. 14 for both substations. The results show that the minimum apparent power flows after DR are decreased to 2.2 and 1.3 MVA for substations A and B respectively. The maximum apparent power flows after DR are increased to 14.9 and 13.7 MVA for substations A and B respectively. It can be seen that even after adopting the DR and new devices, the maximum apparent power flows are 50% and 46% of the combined transformer power ratings of substations A and B respectively.

**Figure 14.** Apparent power flows through transformers after the introduction of DR scheme for scenario 5

Secondary voltages at transformers of both substations after the introduction of DR scheme are presented in Fig. 15a. It can be seen that the minimum and maximum voltages after DR at transformers in substation A are 0.875 p.u. and 0.965 p.u., respectively. For transformers at substation B, these values are 0.862 p.u. and 0.968 p.u., respectively. It can be seen that there are instances when the voltages are 12.5% and 13.8% below the nominal voltages for transformers at substations A and B, respectively.

**Figure 15.** (a) Secondary voltage at transformers of both substations and (b) increment in apparent power flow through inter-connectors after the implementation of DR for scenario 5
The apparent power flows through the interconnectors after the implementation of DR are analysed. It is found that the maximum apparent power flow at the interconnector after DR is decreased by 2.9%. The increment in the apparent power flow through the inter-connectors after the implementation of DR is also plotted in Fig. 15b.

5.6. Scenario 6: Winter, DR 40%, EV 15%

The increments in the total power demand by 15,000 households over a 24 hour period due to the adoption of DR and new devices are computed for winter month when 40% of the households of the study region adopt DR and 15% adopt an EV. It is found that there is an energy demand increment of 50 MWh/day. However, due to the decarbonization, CO₂ emissions reduction of 18 tons/day and average reduction in bills of 33% are achieved by the participating households for this scenario.

The apparent power flows through transformers after implementing DR are plotted in Fig. 16 for both substations. The results show that the minimum apparent power flows after DR are decreased to 2.1 and 1.3 MVA for substations A and B respectively. The maximum apparent power flows after DR are increased to 15.8 and 14.6 MVA for substations A and B respectively. It can be seen that even after adopting the DR and new devices, the maximum apparent power flows are 53% and 49% of the combined transformer power ratings of substations A and B respectively.

![Apparent power flows through transformers after the introduction of DR scheme](image1)

**Figure 16.** Apparent power flows through transformers after the introduction of DR scheme in the study region for scenario 6

Secondary voltages at transformers of both substations after the introduction of the DR scheme are presented in Fig. 17a. It can be seen that the minimum and maximum voltages after DR at transformers in substation A are 0.868 p.u. and 0.966 p.u., respectively. For transformers at substation B, these values are 0.853 p.u. and 0.968 p.u. respectively. It can be seen that there are instances when the voltages are 13.2% and 14.6% below the nominal voltages for transformers at substations A and B, respectively.

![Secondary voltage at transformers of both substations](image2)

**Figure 17.** (a) Secondary voltage at transformers of both substations and (b) increment in apparent power flow through inter-connectors after the implementation of DR for scenario 6
The apparent power flows through the interconnectors after the implementation of DR are analysed. It is found that the maximum apparent power flow at the interconnectors after DR is decreased by 2.9%. The increment in the apparent power flow through the interconnectors after the implementation of DR is also plotted in Fig. 17b.

5.7. Sensitivity Analysis

In this section, we briefly discuss the sensitivity of key variables to changes in the assumed adoption level of the DR scheme, changes in the assumed adoption level of electric vehicles, and also with respect to the season.

Fig. 18a shows that the increment in electricity demand increases linearly with the level of adoption of the DR scheme, as do the CO\textsubscript{2} emissions reductions and maximum transformer loading at the substations. Moreover, the minimum voltage level at the secondary of the transformers at substations decreases with increase in the level of adoption of the DR scheme. A similar sensitivity is noted with changes in the level of adoption of electric vehicles, as shown in Fig. 18b.

![Sensitivity of key variables with respect to the level of adoption of the DR scheme for winter and EV adoption level at 10%](image)

![Sensitivity of key variables with respect to the season for DR adoption level at 40% and EV adoption level at 10%](image)

**Figure 18.** Sensitivity of key variables with respect to the level of adoption of the (a) DR scheme for winter and EV adoption level at 10% and (b) EV for winter and DR adoption level at 40%.

Fig. 19 shows that the electricity demand due to the demand response scheme and new devices increases significantly from summer to winter, as does the maximum transformer loading at the substations. The minimum voltage at the secondary of transformers at substations decreases visibly. It can also be seen that the CO\textsubscript{2} emissions reduction is higher in summer due to higher solar electricity generation.

The results will also be sensitive to many of the assumptions and choices made, including for example the choice of the objective function for DR optimisation, the time of use tariff, and the export price of electricity. These are pre-determined by the user and within the reported scenarios remain fixed.

![Sensitivity of key variables with respect to the season for DR adoption level at 40% and EV adoption level at 10%](image)

**Figure 19.** Sensitivity of key variables with respect to the season for DR adoption level at 40% and EV adoption level at 10%.
5.8. Discussion

As a case study, the effects of applying a DR scheme in households located in the West Wight area of the IoW are investigated. The estimated total power demand by 15,000 households in the study region after implementing DR is compared against the original estimated power demand before DR. The increment in the total power demand is calculated, and its effects at key voltages and power flows are determined using a model of the distribution network of the IoW and a load flow software tool. Specifically, secondary voltages and power flows through the transformers located at substations after the introduction of the DR scheme are computed. Moreover, the apparent power flows through interconnectors between the IoW and the mainland after the implementation of DR are analysed, and the increment in the total apparent power flow is reported. The corresponding CO₂ emissions reduction and reduction in energy/fuel bills for the participating households are also computed. The results show that:

- An average reduction in energy/fuel bills of 60% per annum can be achieved if 40% of the households adopt DR and 10% adopt an EV.
- The respective increments in the total electricity demands are 28, 44 and 59 MWh/day in winter if 20%, 40% and 60% of the households adopt DR and 10% adopt an EV. The corresponding CO₂ emissions reductions are 10, 16 and 22 tons per day.
- The respective increment in the total electricity demand is 44 MWh/day in winter and a decrement is 19 MWh/day in summer if 40% of the households adopt DR and 10% adopt an EV. The corresponding CO₂ emissions reductions are 16 and 23 tons per day.
- The respective increments in the total electricity demands are 37, 44 and 50 MWh/day in winter if 5%, 10% and 15% of the households adopt an EV and 40% adopt DR. The corresponding CO₂ emissions reductions are 14, 16 and 18 tons per day.
- After implementing the DR scheme, the respective maximum apparent power flows through transformers are 35%, 51% and 69% of the combined transformer power rating for 20%, 40% and 60% DR adoption scenarios.
- There are instances when the secondary voltages are 9.4%, 14.1% and 20.2% below the nominal voltages for transformers at substations for 20%, 40% and 60% DR adoption scenarios. These voltages are clearly not acceptable from an operational perspective, but there are relatively easy ways of bringing those voltages to the allowed range of +/- 6% of the nominal voltage, including the adjustment of transformer taps and the use of reactive compensation.
- The maximum apparent power flows through the interconnectors after DR are decreased by 0.8%, 2.2% and 3.6% for 20%, 40% and 60% DR adoption scenarios.
- Aggregated power export from the participating households after the implementation of DR is also estimated. It is noted that for scenario 2 (summer, 40% adoption of DR, 10% adoption of EV), the peak value of export is about 6.4MW, which is about 10% of the installed large-scale solar PV generation capacity on the island.

Through utilizing a community wide area with multiple household sizes and various compositions of DR technologies this work builds upon the current literature focusing primarily on single technologies within an individual domestic setting [2, 3, 4, 5, 8]. This work highlights the positive impact that integrating intelligent DR systems can have on operating costs and GHG emissions on a community scale.

Within the model presented, several key limitations exist concerning the EV charging infrastructure. At present the model does not consider vehicle charging and discharging during the day when there is peak supply of renewable generation and the ability to utilize excess stored capacity, reducing the need to charge during the night when renewable output diminishes. This model does not address the embedded CO₂ and financial/economic costs associated with the removal of non-DSR technologies and the installation of new equipment.
6. Conclusions

In the current work, a two-stage optimisation DR model applied to complete households is described. The model incorporates multiple potential DR functions that have been widely reported within the literature: electric vehicles (EV), rooftop PV, the ability to export electricity to generate revenue, time of use tariffs, household battery bank, electric storage heaters, immersion water heaters, smart meters and DR controller. This DR model can be used to provide valuable information for energy systems decision and policy makers, particularly when used to analyse the systemic effects of possible future national or regional policies and technologies.

Within the IoW EAC case study two main conclusions can be drawn:

- All scenarios showed a reduction in energy/transport fuel-bills of between 23% and 93%. Within the case study outputs, it is clear that increasing EV ownership can lead to a greater reduction in overall combined energy costs, particularly in the summer season. This is likely due to a combined ability to generate a revenue through the export of excess energy that offsets total costs, with a reduction in fuel costs of electric compared to fossil fuels. At present, it is not possible to differentiate the savings made by DR only and EV & DR customers.

- All scenarios demonstrate a reduction in the climate impacts with between 10 to 23 tons per day of CO\text{\textsubscript{e}} between the interventions. It is likely that that EV owners experience both a greater saving on total fuel bills and a greater reduction in CO\text{\textsubscript{e}} emissions, although at present it is not possible to directly differentiate between the different participants infrastructure.

This work demonstrates the potential beneficial impacts that a DR can have both for the customer in terms of financial savings and for the community at large through the reduction in GHG emissions. Minimal uptake enabled savings is exhibited by all engaged customers, showing that there is scalability in the integration of these methodologies and is not dependent on a significant initial uptake.

The DR modelling approach is deterministic and does not account for uncertainty in the model input, and only considers uncertainty through the uptake rate of DR and EV ownership within the communities. This can be improved through the implementation of stochastic analysis, although this would also require significantly more data on input variables and would become computationally intensive due to the non-linear aspect of the model. The current model can enable dynamic pricing based on generation and demand profiles. However, in this instance, the values are fixed as the pricing is outside of the remit of this study. The model and the case study currently do not consider the following: embedded costs/ CO\text{\textsubscript{e}} of new technologies, dynamic EV charging/ discharge and the virtual power plant model. Future work will enable the integration of these functions, with the ability to disaggregate customer types to determine how both EV and non-EV owners benefit, as well as prosumer/ non-prosumer members. Future iterations will also enable the input of commercial and industrial consumers as well as community and local energy production schemes.


Funding: This research received funding from Innovate UK Smart Local Energy Systems Concepts 133798, - project entitled “Isle Of Wight Energy Autonomous Community” (Grant Number: 17660).

Acknowledgments: The valuable inputs and thoughtful conversations with the project partner Tereza Borges (Lumenaza GmBH) and other project partners are greatly acknowledged.

Conflicts of Interest: The authors declare no conflict of interest.

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